

## Reactive Action Programs

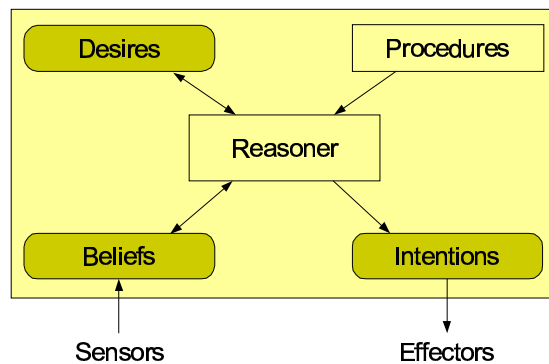
- BDI-Agents
- Programming in AgentSpeak
- AgentSpeak in Prolog
- The SPARK Programming Language

## BDI-Agents

The state of an agent at any time is characterized by its

- **Beliefs**, which constitute the internal world model. They describe what the agent currently believes about the environment and its own tasks.
- **Desires**, which are derived from the beliefs and describe what the agent currently tries to achieve.
- **Intentions**, which are the behaviors (procedures) which the agent has adopted and is currently following in order to meet its desires.

## Procedural Reasoning Systems (PRS)



## Beliefs

- Beliefs are composed of fluents
- Beliefs are affected by actions and sensor information
- Beliefs may include static knowledge (aka domain constraints)
- Beliefs may also concern the "behavioral stance" of the agent

## Desires

- Desires are properties which the agent currently wants to achieve
- Desires are (typically short-term) goals

## Procedures

- Procedures constitute the behavioral knowledge of the agent
- Procedures correspond to (typically short) GOLOG procedures or ALP clausal definitions
- Each procedure has as condition a desire for which it is suitable

## Intentions

- Intentions are instantiated procedures which the agent has selected to meet its desires
- Intentions can be active or passive
- Actions are selected from active intentions
- Intention ordering: Intentions on top are active, all others remain passive until the preceding intentions have been completed

## Reasoner

- Controls the execution of a reactive action program
- **Sense-Select-Act** cycle
  - Sense the environment
  - Select procedures for desires; select an active intention
  - Act according to the selected intention

# AgentSpeak

# Syntax

## Definition 6.2.1

An **AgentSpeak domain signature** includes a finite set of belief predicates and a finite set of action predicates.

A **belief literal** is an atom with a belief predicate or its negation.

## Example: Gold Mining with Moving Obstacles

Symbol	Type	
<i>Adjacent</i>	$\text{CELL} \times \text{CELL}$	$\text{Adjacent}(A, B)$
<i>At</i>	$\{\text{Agent, Gold, Obstacle, Depot}\} \times \text{CELL}$	$\text{Adjacent}(B, C)$
<i>Carries</i>	$\{\text{Agent}\} \times \{\text{Gold}\}$	$\text{At}(\text{Agent}, A)$

$\text{At}(\text{Gold}, B)$   
 $\text{At}(\text{Depot}, C)$

Symbol	Type	Meaning
<i>Pick</i>	$\{\text{Gold}\}$	pick up a gold item
<i>Drop</i>	$\{\text{Gold}\}$	drop a gold item
<i>Move</i>	$\text{CELL} \times \text{CELL}$	move to an adjacent cell

## Triggering Events

### Definition 6.2.2

If  $f$  is a belief atom, then  $\neg f$  and  $?f$  are **goals**.

A **triggering event** is any of

- $+f$
- $-f$
- $+g$
- $-g$

where  $f$  belief atom,  $g$  goal.

## Procedures

### Definition 6.2.2 (cont'd)

A **procedure** is an expression

$$e : b_1, \dots, b_m \leftarrow p_1, \dots, p_n$$

where

- $e$  triggering event
- **context**  $b_1, \dots, b_m$  belief literals ( $m \geq 0$ )
- **body**  $p_1, \dots, p_n$  action atoms or goals ( $n \geq 0$ )

Empty context or body denoted by *True*

## Example

$+At(Gold, x) : At(Agent, x), At(Depot, y) \leftarrow Pick(Gold), !At(Agent, y), Drop(Gold)$

$+!At(Agent, x) : At(Agent, x) \leftarrow True$

$+!At(Agent, x) : At(Agent, y), x \neq y, Adjacent(y, z), \neg At(Obstacle, z) \leftarrow Move(y, z), !At(Agent, x)$

## Operational Semantics

State of AgentSpeak program characterized by triple

- $\mathcal{B}$ : a set of variable-free belief atoms
- $\mathcal{I}$ : a set of intentions of the form  $[P_1; \dots; P_n]$  where each  $P_i$  procedure body (possibly partially instantiated)
- $\mathcal{D}$ : a set of desires of the form  $\langle e; i \rangle$  where  $e$  triggering event,  $i$  intention  
**External** desire:  $\langle e; [] \rangle$

## Selection Functions

- $S_D$  selects an element from the current desires
- $S_I$  selects an element from the current intentions
- $S_P$  selects an applicable procedure for a triggering event

## Relevance / Applicability

### Definition 6.2.3

$\mathcal{B}$  – set of variable-free belief atoms

$e$  – triggering event

$P$  – procedure  $d : b_1, \dots, b_m \leftarrow p_1, \dots, p_n$

$P$  **relevant** for  $e : \Leftrightarrow d\theta = e\theta$  for some  $\theta$

$P\theta\eta$  **applicable** to  $e$  wrt.  $\mathcal{B} : \Leftrightarrow \mathcal{B} \vdash (b_1 \wedge \dots \wedge b_m)\theta\eta$

## Example

$Adjacent(A, B)$

$Adjacent(B, C)$

$At(Agent, A)$

$At(Gold, A)$

$At(Depot, C)$

$+!At(Agent, x) : At(Agent, x) \leftarrow True$

$+!At(Agent, x) : At(Agent, y), x \neq y, Adjacent(y, z), \neg At(Obstacle, z)$

$\leftarrow Move(y, z), !At(Agent, x)$

Both procedures are relevant for  $+!At(Agent, C)$ .

The second procedure is also applicable with  $\theta = \{x/C\}$  and  $\eta = \{y/A, z/B\}$

## Derivations: States

$\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \sigma \rangle$  state, where  $\sigma \in \{\text{Sense, Select, Act}\}$

$\langle \mathcal{B}, \emptyset, \emptyset, \text{Sense} \rangle$  initial state

## Derivation Rules (1)

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Sense} \rangle}{\langle \mathcal{B}', \mathcal{D}', \mathcal{I}, \text{Select} \rangle}$$

$\mathcal{B}' : \Leftrightarrow \mathcal{B}$  updated according to sensing result

$\mathcal{D}' : \Leftrightarrow \mathcal{D}$  plus external desires that have been sensed

### Derivation Rules (2)

$$\frac{\langle \mathcal{B}, \{\}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \{\}, \mathcal{I}, \text{Act} \rangle}$$

If  $S_D(\mathcal{D}) = \langle e; \uparrow \rangle$  and no relevant procedure exists:

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{e; i\}, \mathcal{I}, \text{Select} \rangle}$$

If  $S_D(\mathcal{D}) = \langle e; \uparrow \rangle$  and relevant but not applicable procedures exist:

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}$$

### Derivation Rules (3)

If  $S_D(\mathcal{D}) = \langle e; \uparrow \rangle$  and  $S_P(e) = P\theta\eta$ :

(a) For external desires

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{e; \uparrow\}, \mathcal{I} \cup \{P\theta\eta\}, \text{Act} \rangle}$$

(b) For internal desires

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{e; i\}, \mathcal{I} \cup \{P\theta\eta; P_1; \dots; P_k\}, \text{Act} \rangle}$$

where  $i = [P_1, \dots, P_k]$

### Derivation Rules (4)

$$\frac{\langle \mathcal{B}, \mathcal{D}, \{\}, \text{Act} \rangle}{\langle \mathcal{B}, \mathcal{D}, \{\}, \text{Sense} \rangle}$$

If  $S_I(\mathcal{I}) = [a, P_1; \dots; P_k]$ :

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle \mathcal{B}', \mathcal{D}, \mathcal{I} \setminus \{a, P_1; \dots; P_k\} \cup \{P_1; \dots; P_k\}, \text{Sense} \rangle}$$

$\mathcal{B}' := \mathcal{B}$  updated according to effects of  $a$

### Derivation Rules (5)

If  $S_I(\mathcal{I}) = [!f, P_1; \dots; P_k]$ :

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle \mathcal{B}, \mathcal{D} \cup \{(!f; P_1; \dots; P_k)\}, \mathcal{I} \setminus \{!f, P_1; \dots; P_k\}, \text{Sense} \rangle}$$

If  $S_I(\mathcal{I}) = [?f, P_1; \dots; P_k]$  and  $\mathcal{B} \vdash f\theta$  for some  $\theta$ :

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{?f, P_1; \dots; P_k\} \cup \{P_1; \dots; P_k\}\theta, \text{Sense} \rangle}$$

If  $S_I(\mathcal{I}) = [?f, P_1; \dots; P_k]$  and  $\mathcal{B} \not\vdash f\theta$  for all  $\theta$ :

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle \mathcal{B}, \mathcal{D} \cup \{(?f; P_1; \dots; P_k)\}, \mathcal{I} \setminus \{?f, P_1; \dots; P_k\}, \text{Sense} \rangle}$$

## Derivation Rules (6)

If  $S_i(I) = [True; P_2; \dots; P_k]$ :

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, Act \rangle}{\langle B, \mathcal{D}, \mathcal{I} \setminus \{True; P_2; \dots; P_k\} \cup \{P_2; \dots; P_k\}, Sense \rangle}$$

If  $S_i(I) = []$ :

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, Act \rangle}{\langle B, \mathcal{D}, \mathcal{I} \setminus \{[]\}, Sense \rangle}$$

## Example

$B = \{At(Agent, A), At(Gold, A), At(Depot, C)\}$

$\mathcal{D} = \{ \langle +At(Gold, A); [] \rangle \}$

$\mathcal{I} = \{ \}$

$\sigma = Select$

---

$B = \{At(Agent, A), At(Gold, A), At(Depot, C)\}$

$\mathcal{D} = \{ \}$

$\mathcal{I} = \{ \langle !Pick(Gold), !At(Agent, C), Drop(Gold) \rangle \}$

$\sigma = Act$

---

$B = \{At(Agent, A), Carries(Agent, Gold), At(Depot, C)\}$

$\mathcal{D} = \{ \}$

$\mathcal{I} = \{ \langle !At(Agent, C), Drop(Gold) \rangle \}$

$\sigma = Sense$

## Example (cont'd)

---

$B = \{At(Agent, A), Carries(Agent, Gold), At(Depot, C)\}$

$\mathcal{D} = \{ \}$

$\mathcal{I} = \{ \langle !At(Agent, C), Drop(Gold) \rangle \}$

$\sigma = Select$

---

$B = \{At(Agent, A), Carries(Agent, Gold), At(Depot, C)\}$

$\mathcal{D} = \{ \}$

$\mathcal{I} = \{ \langle !At(Agent, C), Drop(Gold) \rangle \}$

$\sigma = Act$

---

$B = \{At(Agent, A), Carries(Agent, Gold), At(Depot, C)\}$

$\mathcal{D} = \{ \langle +!At(Agent, C); [Drop(Gold)] \rangle \}$

$\mathcal{I} = \{ \}$

$\sigma = Sense$

## An AgentSpeak Interpreter

```

desire(E,I) :- procedure(E,P), intention([P|I]).
intention([[do(A)|P]|I]) :- do(A), intention([P|I]).
intention([[!(F)|P]|I]) :- desire(+!(F), [P|I]).
intention([[?(F)|P]|I]) :- F, intention([P|I]).
intention([[?(F)|P]|I]) :- desire(+?(F), [P|I]).
intention([[|I]) :- intention(I).
intention([]).
    
```

## Example AgentSpeak Program (1)

```
adjacent(a,b).
adjacent(b,c).
at(agent,a).
at(gold,a).
at(depot,c).

do(pick(gold)) :- at(agent,X), retract(at(gold,X)),
                 assert(carries(agent,gold)).
do(move(X,Y)) :- at(agent,X), retract(at(agent,X)),
                 assert(at(agent,Y)).
do(drop(gold)) :- at(agent,X), retract(carries(agent,gold)).
```

## Example AgentSpeak Program (2)

```
procedure(+ (at(gold,X)),P) :-
    at(agent,X), at(depot,Y),
    P = [do(pick(gold)), !(at(agent,Y)), do(drop(gold))].

procedure(+ (! (at(agent,X))),P) :- at(agent,X), P=[].

procedure(+ (! (at(agent,X))),P) :-
    at(agent,Y), not X=Y, adjacent(Y,Z), not at(obstacle,Z),
    P = [do(move(Y,Z)), !(at(agent,X))].
```

## Example: Query `desire(+ (at(gold,a)), [])`

```
[[do(pick(gold)), !(at(agent,c)), do(drop(gold))]]
[[!(at(agent,c)), do(drop(gold))]]
[[do(move(a,b)), !(at(agent,c)), [do(drop(gold))]]
[[!(at(agent,c)), [do(drop(gold))]]
[[do(move(b,c)), !(at(agent,c)), [], [do(drop(gold))]]
[[!(at(agent,c)), [], [do(drop(gold))]]
[[[], [], [], [do(drop(gold))]]
[[[], [], [do(drop(gold))]]
[[[], [do(drop(gold))]]
[[do(drop(gold))]]
[[]]
[]
```

## Programming in SPARK



## The SPARK System

SPARK – Stanford Research Institute Procedural Agent Realization Kit

- Large-scale, practical applications of reactive agent programs
- BDI-model, PRS-architecture (like AgentSpeak)
- More expressive means to control agents in rich and dynamic domains

## SPARK Syntax

- **Belief literals** : $\Leftrightarrow$  belief atoms or their negation
- **Actions** : $\Leftrightarrow$  primitive actions or names for complex behaviors
- Pre-defined belief atoms are:
  - *Desire*(*a*)            where *a* action
  - *Success*(*a*)            where *a* action
  - *Fail*(*a*)                where *a* action
  - *Desire*( $\varphi$ )            where  $\varphi$  belief literal
  - *Success*( $\varphi$ )            where  $\varphi$  belief literal
  - *Fail*( $\varphi$ )                where  $\varphi$  belief literal

## Triggers and Procedures

- **Triggers** are of the form
  - *Do*(*a*)                where *a* action
  - *Achieve*( $\varphi$ )        where  $\varphi$  belief literal
  - + $\varphi$                     where  $\varphi$  belief literal
- **Procedures** are of the form
  - $e : \phi \leftarrow \tau$
  - where *e* trigger,  $\phi$  formula using belief atoms,  $\tau$  task description

## Programming Language for Task Descriptions

Task	Meaning
<b>noop</b>	do nothing
<b>fail</b>	fail
<b>conclude</b> $\varphi$	add the fact to the beliefs
<b>retract</b> $\varphi$	delete the fact from the beliefs
<b>do</b> <i>a</i>	perform the action
<b>achieve</b> $\varphi$	attempt to achieve $\varphi$
<b>seq</b> ( $\tau_1, \tau_2$ )	execute $\tau_1$ then $\tau_2$
<b>if</b> ( $\varphi, \tau_1, \tau_2$ )	if $\varphi$ is true, execute $\tau_1$ , else $\tau_2$
<b>try</b> ( $\tau, \tau_1, \tau_2$ )	if $\tau$ succeeds, execute $\tau_1$ , else $\tau_2$
<b>wait</b> ( $\varphi, \tau$ )	wait until $\varphi$ is true, then execute $\tau$
<b>while</b> ( $\varphi, \tau_1, \tau_2$ )	repeat $\tau_1$ until $\varphi$ has no solution, then execute $\tau_2$

## Example Procedures

```
Do(ForwardMessage(x)) : ¬IsSpam(x) ← try ( achieve ClassifyMessage(x,y),
                                         do AddToFolder(x,y),
                                         do Forward(x)
                                         )
```

```
Do(ForwardMessage(x)) : IsSpam(x) ← do Delete(x)
```

## Operational Semantics: State Transitions

- Semantics of a task description given by a finite automaton
- Distinguished states in this automaton:
  - $s_0$  initial state
  - $s^+$  success state
  - $s^-$  failure state
- Labeled state transitions

$$s \xrightarrow{\vec{c}|\vec{e}} s'$$

## Conditions and Effects

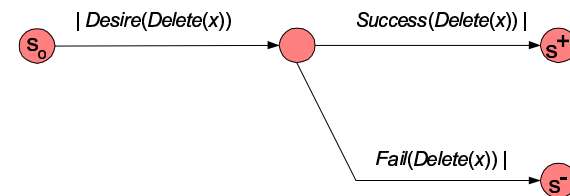
In a labeled state transition  $s \xrightarrow{\vec{c}|\vec{e}} s'$ , the

- conditions**  $\vec{c} = c_1, \dots, c_n$  are
  - $c_i = \varphi$  presence of belief literal  $\varphi$
  - $c_i = \bar{\varphi}$  absence of belief literal  $\varphi$
- effects**  $\vec{e} = e_1, \dots, e_m$  are
  - $e_i = \varphi$  addition of belief atom  $\varphi$
  - $e_i = \bar{\varphi}$  removal of belief atom  $\varphi$

Empty conditions and/or effects are simply omitted

## Example (1)

```
Do(ForwardMessage(x)) : IsSpam(x) ← do Delete(x)
```



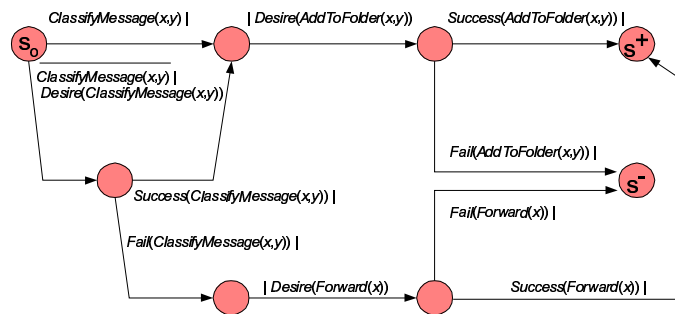
## Recursive Construction of State Machine

$$\begin{aligned} \mathcal{M}(\text{noop}) &:\Leftrightarrow \{s_0 \rightarrow s^+\} \\ \mathcal{M}(\text{fail}) &:\Leftrightarrow \{s_0 \rightarrow s^-\} \\ \mathcal{M}(\text{conclude } \varphi) &:\Leftrightarrow \{s_0 \xrightarrow{|\varphi} s^+\} \\ \mathcal{M}(\text{retract } \varphi) &:\Leftrightarrow \{s_0 \xrightarrow{|\overline{\varphi}} s^+\} \\ \mathcal{M}(\text{do } a) &:\Leftrightarrow \{s_0 \xrightarrow{|\text{Desire}(a)} s, s \xrightarrow{\text{Success}(a)} s^+, s \xrightarrow{\text{Fail}(a)} s^-\} \\ \mathcal{M}(\text{achieve } \varphi) &:\Leftrightarrow \{s_0 \xrightarrow{|\varphi} s^+, s_0 \xrightarrow{|\overline{\varphi}|\text{Desire}(\varphi)} s, s \xrightarrow{\text{Success}(\varphi)} s^+, s \xrightarrow{\text{Fail}(\varphi)} s^-\} \end{aligned}$$

## Construction of State Machine (cont'd)

$$\begin{aligned} \mathcal{M}(\text{seq}(\tau_1, \tau_2)) &:\Leftrightarrow \mathcal{M}(\tau_1)\{s^+/s\} \cup \mathcal{M}(\tau_2)\{s_0/s\} \\ \mathcal{M}(\text{if } (\varphi, \tau_1, \tau_2)) &:\Leftrightarrow \varphi \Rightarrow \mathcal{M}(\tau_1) \cup \overline{\varphi} \Rightarrow \mathcal{M}(\tau_2) \\ \mathcal{M}(\text{try } (\tau, \tau_1, \tau_2)) &:\Leftrightarrow \mathcal{M}(\tau)\{s^+/s_1, s^-/s_2\} \cup \mathcal{M}(\tau_1)\{s_0/s_1\} \cup \mathcal{M}(\tau_2)\{s_0/s_2\} \\ \mathcal{M}(\text{wait } (\varphi, \tau)) &:\Leftrightarrow \{s_0 \rightarrow s\} \cup \varphi \Rightarrow \mathcal{M}(\tau)\{s_0/s\} \\ \mathcal{M}(\text{while } (\varphi, \tau_1, \tau_2)) &:\Leftrightarrow \{s_0 \rightarrow s\} \cup \varphi \Rightarrow \mathcal{M}(\tau_1)\{s_0/s, s^+/s\} \cup \overline{\varphi} \Rightarrow \mathcal{M}(\tau_2)\{s_0/s\} \end{aligned}$$

## Example (2)



## Derivations

- $\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \sigma \rangle$  state
- $\mathcal{B}$  set of belief literals
  - $\mathcal{D}$  set of  $\text{Desire}(a)$ ,  $\text{Desire}(\varphi)$ , or  $+ \varphi$
  - $\mathcal{I}$  set of triples  $\langle d, S, s \rangle$ 
    - $d$  desire
    - $S$  state machine instance
    - $s$  current state in  $S$
  - $\sigma \in \{\text{Sense}, \text{Select}, \text{Act}\}$
- $\langle \mathcal{B}, \emptyset, \emptyset, \text{Sense} \rangle$  initial state

## Selection Functions

- $S_D$  selects an element from the current desires
- $S_p$  selects an applicable procedure for a desire
- $S_s$  selects an element  $\langle d, S, s_1 \rangle \in \mathcal{I}$  with an allowed state transition  $s_1 \xrightarrow{d} s_2$

## Derivation Rules (1)

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Sense} \rangle}{\langle \mathcal{B}', \mathcal{D}', \mathcal{I}, \text{Select} \rangle}$$

$\mathcal{B}' : \Leftrightarrow \mathcal{B}$  updated according to sensing result

$\mathcal{D}' : \Leftrightarrow \mathcal{D}$  plus all sensed desires

## Derivation Rules (2)

$$\frac{\langle \mathcal{B}, \{\}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \{\}, \mathcal{I}, \text{Act} \rangle}$$

If  $S_D(\mathcal{D}) = \text{Desire}(x)$  and there is applicable procedure for  $Do(a)$  (if  $x = a$ ) or

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle \quad \text{Achieve}(\varphi) \text{ (if } x = \varphi\text{)}}{\langle \mathcal{B}, \mathcal{D} \setminus \{\text{Desire}(x)\}, \mathcal{I} \cup \{\langle \text{Desire}(x), S, s_0 \rangle\}, \text{Act} \rangle}$$

where  $S$  state machine from  $S_p(\text{Desire}(x))$

If  $S_D(\mathcal{D}) = \text{Desire}(x)$  and no procedure applicable:

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{\text{Desire}(x)\}, \mathcal{I} \cup \{\langle \text{Desire}(x), S, s_0 \rangle\}, \text{Act} \rangle}$$

where  $S = \{s_0 \xrightarrow{\text{Fail}(x)} s^+\}$

## Derivation Rules (3)

If  $S_D(\mathcal{D}) = +\varphi$  and there is applicable procedure:

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{+\varphi\}, \mathcal{I} \cup \mathcal{I}', \text{Act} \rangle}$$

where  $\mathcal{I}' : \Leftrightarrow$  all  $\langle +\varphi, S, s_0 \rangle$  for applicable procedures

If  $S_D(\mathcal{D}) = +\varphi$  and no applicable procedure:

$$\frac{\langle \mathcal{B}, \mathcal{D}, \mathcal{I}, \text{Select} \rangle}{\langle \mathcal{B}, \mathcal{D} \setminus \{+\varphi\}, \mathcal{I}, \text{Select} \rangle}$$

### Derivation Rules (4)

$$\frac{\langle B, \mathcal{D}, \{\}, \text{Act} \rangle}{\langle B, \mathcal{D}, \{\}, \text{Sense} \rangle}$$

If  $S_i(\mathcal{I})$  is  $\langle d, S, s_i \rangle$  along with  $s_1 \stackrel{\text{dLE}}{\rightarrow} s_2$ :

a) If  $s_2 \notin \{s^+, s^-\}$

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle B', \mathcal{D}', \mathcal{I} \setminus (\langle d, S, s_1 \rangle \cup \langle d, S, s_2 \rangle), \text{Sense} \rangle}$$

b) If  $d = +\varphi$  and  $s_2 \in \{s^+, s^-\}$ :

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle B', \mathcal{D}', \mathcal{I} \setminus \langle d, S, s_1 \rangle, \text{Sense} \rangle}$$

### Derivation Rules (5)

c) If  $d = \text{Desire}(x)$  and  $s_2 = s^+$

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle B' \cup \{\text{Success}(x)\}, \mathcal{D}', \mathcal{I} \setminus \langle d, S, s_1 \rangle, \text{Sense} \rangle}$$

d) If  $d = \text{Desire}(x)$  and  $s_2 = s^-$

$$\frac{\langle B, \mathcal{D}, \mathcal{I}, \text{Act} \rangle}{\langle B' \cup \{\text{Fail}(x)\}, \mathcal{D}', \mathcal{I} \setminus \langle d, S, s_1 \rangle, \text{Sense} \rangle}$$