

# Integrated Logic Systems

## Part 2: Prolog (II)

- Compiling  $L_0$ -programs
- Unification
- From  $L_0$  to  $L_1$ : handling atoms
- Special data structures: constants and lists

# Compiling a Program

The flattened equations need to be ordered

$$X_1 = f_1(\vec{X}_1), \dots, X_k = f_k(\vec{X}_k)$$

such that no  $X_i$  occurs in  $\vec{X}_{i+1}, \dots, \vec{X}_k$

An equation  $X_i = f(X_{i_1}, \dots, X_{i_n})$  is processed as:

1. `get structure f/n, Xi`
2. `unify variable Xi1 or unify value Xi1`
- ⋮
- n+1. `unify variable Xin or unify value Xin`

`unify_variable Xi` used if  $X_i$  has not been processed before

`unify_value Xi` used if  $X_i$  has been processed before

# Dereferencing (Through a Chain of Variable References)

```
function deref(a: address): address;  
begin  
    ⟨ tag,value ⟩ ← STORE[a];  
if (tag=REF) ∧ (value ≠ a)  
    then return deref (value)  
    else return a  
end deref
```

# WAM<sub>0</sub> Machine Instructions (II)

```
get_structure f/n, Xi ≡ addr ← deref (Xi);  
    case STORE[addr] of  
        ⟨REF, _⟩ : HEAP[H] ← ⟨STR, H+1⟩;  
                HEAP[H+1] ← f/n;  
                bind(addr, H);  
                H ← H+2;  
                mode ← write;  
        ⟨STR, a⟩ : if HEAP[a] = f/n  
                then  
                    begin  
                        S ← a+1;  
                        mode ← read  
                    end  
                else fail ← true;  
        other: fail ← true;  
    endcase
```

# Binding in WAM<sub>0</sub>

```
procedure bind( $a_1, a_2$ : address);  
    begin  
        case  $\leftarrow$  STORE[ $a_1$ ] of  
             $\langle$  REF,  $\_$   $\rangle$  : STORE[ $a_1$ ]  $\leftarrow$  STORE[ $a_2$ ];  
            other      : STORE[ $a_2$ ]  $\leftarrow$  STORE[ $a_1$ ];  
        endcase;  
    end bind
```

# WAM<sub>0</sub> Machine Instructions (III)

`unify_variable`  $X_i \equiv$  **case mode of**  
    read:  $X_i \leftarrow \text{HEAP}[S];$   
    write:  $\text{HEAP}[H] \leftarrow \langle \text{REF}, H \rangle;$   
           $X_i \leftarrow \text{HEAP}[H];$   
           $H \leftarrow H+1;$   
    **endcase;**  
     $S \leftarrow S+1$

`unify_value`  $X_i \equiv$  **case mode of**  
    read: *unify* ( $X_i, S$ );  
    write:  $\text{HEAP}[H] \leftarrow X_i;$   
           $H \leftarrow H+1;$   
    **endcase;**  
     $S \leftarrow S+1$

# Unification (Part I)

```
procedure unify( $a_1, a_2$ : address);  
  begin  
    push( $a_1$ , PDL); push( $a_2$ , PDL);  
    fail  $\leftarrow$  false;  
    while  $\neg$ (empty(PDL)  $\vee$  fail) do  
      begin  
         $d_1 \leftarrow$  deref(pop(PDL));  $d_2 \leftarrow$  deref(pop(PDL));  
        if  $d_1 \neq d_2$  then  
          begin  
             $\langle t_1, v_1 \rangle \leftarrow$  STORE[ $d_1$ ];  
             $\langle t_2, v_2 \rangle \leftarrow$  STORE[ $d_2$ ];  
            if ( $t_1 = \text{REF}$ )  $\vee$  ( $t_2 = \text{REF}$ )  
              then bind( $d_1, d_2$ )  
          end  
        end  
      end  
    end
```

# Unification (Part II)

```
else
  begin
     $f_1 / n_1 \leftarrow \text{STORE}[v_1]; f_2 / n_2 \leftarrow \text{STORE}[v_2];$ 
    if  $(f_1 = f_2) \wedge (n_1 = n_2)$ 
      then
        for  $i \leftarrow 1$  to  $n_1$  do
          begin
             $\text{push}(v_1 + i, \text{PDL});$ 
             $\text{push}(v_2 + i, \text{PDL});$ 
          end
        else  $\text{fail} \leftarrow \text{true}$ 
      end
    end
  end
end unify
```



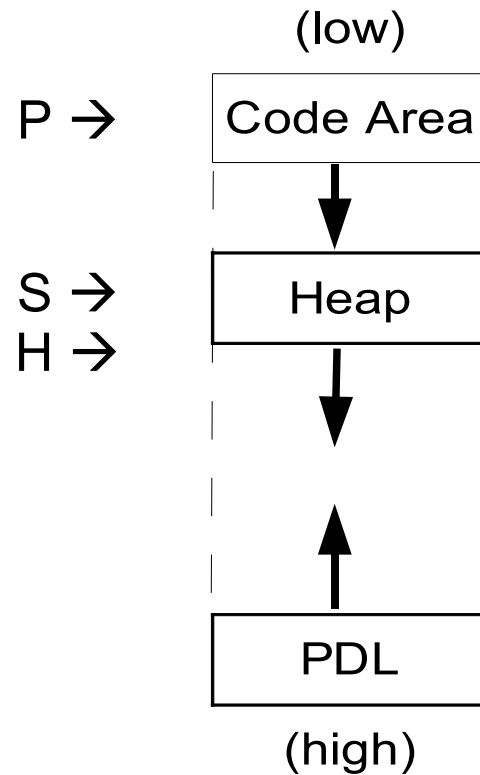
# From $L_0$ to $L_1$

A program is a set of **atoms**, with at most one for each predicate name.

A query is an **atom**.

# WAM<sub>1</sub> Memory Layout

Registers



Term registers:

$X_1, X_2, \dots, X_n, \dots$

# Control Instructions

`call p/n`  $\equiv$   $P \leftarrow @(p/n);$

where  $@(p/n)$  stands for the address in the code area of the instructions for the clause defining predicate  $p/n$ .

If  $p/n$  has not been defined, failure occurs.

`proceed`  $\equiv$  `no-op;` (for the moment)

# Argument Registers

The first  $n$  registers  $X_1, \dots, X_n$  are systematically allocated to the arguments of an  $n$ -ary predicate.

To emphasise this, we write  $A_i$  if  $X_i$  is used as argument register.

Example:  $A_1, A_2, A_3, X_4, X_5, X_6, X_7$  when processing a predicate with 3 arguments

Now also a variable can occur on the right hand side of a flattened equation.

# Instructions for Variables as Roots

- `put_variable  $X_n, A_i$`   
handles a root variable which occurs for the first time in a query
- `put_value  $X_n, A_i$`   
handles a root variable which previously occurred in a query
- `get_variable  $X_n, A_i$`   
handles a root variable which occurs for the first time in a program atom
- `get_value  $X_n, A_i$`   
handles a root variable which previously occurred in a program atom

# WAM<sub>1</sub> Machine Instructions

`put_variable`  $X_n, A_i \equiv \text{HEAP}[H] \leftarrow \langle \text{REF}, H \rangle;$

$X_n \leftarrow \text{HEAP}[H];$

$A_i \leftarrow \text{HEAP}[H];$

$H \leftarrow H+1;$

`put_value`  $X_n, A_i \equiv A_i \leftarrow X_n;$

`get_variable`  $X_n, A_i \equiv X_n \leftarrow A_i;$

`get_value`  $X_n, A_i \equiv \text{unify}(X_n, A_i);$

# Special Datastructures: Heap Representation with Constants

7	STR	8
8	g/1	
9	CON	a
10	STR	11
11	f/2	
12	CON	b
13	STR	8

Heap representation of  
 $f(b, g(a))$

# Instructions for Constants (I): Constants as Arguments

`put_constant c, Ai ≡ Ai ← ⟨CON,c⟩;`

`get_constant c, Ai ≡ addr ← deref(Ai);`

**case** STORE[addr] **of**

    ⟨REF,⟨\_⟩⟩ : STORE[addr] ← ⟨CON,c⟩;

    ⟨CON,c'⟩ : fail ← (c ≠ c');

**other** : fail ← **true**;

**endcase**;



# Instructions for Constants (II): Constants Inside a Term

set\_constant  $c$   $\equiv$  HEAP[H]  $\leftarrow$   $\langle$ CON, $c$  $\rangle$ ;  
H  $\leftarrow$  H+1;

unify\_constant  $c$   $\equiv$  **case mode of**  
     read :  $addr \leftarrow deref(S)$ ;  
         **case STORE[addr] of**  
              $\langle$ REF, $\_$  $\rangle$  : STORE[addr]  $\leftarrow$   $\langle$ CON, $c$  $\rangle$ ;  
              $\langle$ CON, $c'$  $\rangle$  :  $fail \leftarrow (c \neq c')$ ;  
             **other** :  $fail \leftarrow \mathbf{true}$ ;  
         **endcase**;  
     write : HEAP[H]  $\leftarrow$   $\langle$ CON, $c$  $\rangle$ ;  
         H  $\leftarrow$  H+1;  
**endcase**;

# Heap Representation with Lists

1	REF	1	
2	CON	[]	
3	REF	3	← A1
4	REF	3	← A2
5	LIS	1	
6	STR	7	
7	f/1		← A3
8	REF	1	

Heap representation of  
 $p(Z,[Z,W],f(W))$

# Instructions for Lists

put\_list  $X_i$              $\equiv$   $X_i \leftarrow \langle \text{LIS}, H \rangle;$

get\_list  $X_i$              $\equiv$   $addr \leftarrow \text{deref}(X_i);$   
**case** STORE[ $addr$ ] **of**  
     $\langle \text{REF}, \_ \rangle$  : HEAP[H]  $\leftarrow \langle \text{LIS}, H+1 \rangle;$   
                   $bind(addr, H);$   
                   $H \leftarrow H+1;$   
                   $mode \leftarrow \text{write};$   
     $\langle \text{LIS}, a \rangle$  :  $S \leftarrow a;$   
                   $mode \leftarrow \text{read};$   
    **other**        :  $fail \leftarrow \text{true};$   
**endcase;**

# Example: Query $p(Z,[Z,W],f(W))$

```
put_list X5  
set_variable X6  
set_constant []  
put_variable X4,A1  
put_list A2  
set_value X4  
set_value X5  
put_structure f/1,A3  
set_value X6  
call p/3
```

# Example: Fact $p(f(X), [Y, f(a)], Y)$

get\_structure f/1,  $A_1$

unify\_variable  $X_4$

get\_list  $A_2$

unify\_variable  $X_5$

unify\_variable  $X_6$

get\_value  $X_5, A_3$

get\_list  $X_6$

unify\_variable  $X_7$

unify\_structure f/1,  $X_7$

unify\_constant a

proceed

# Objectives

- Compiling  $L_0$ -programs
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