

# Integrated Logic Systems (Part I)

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International Master Program in Computational Logic — summer term 2010

20.04.2010

## Exercise 1.1

Consider  $\mathcal{M}_0$  query term  $Q$ :

$$? - \text{legal}(\text{player}(X), \text{move}(Y, Y))$$

and  $\mathcal{M}_0$  program term  $P$ :

$$\text{legal}(X, \text{move}(\text{cell}(a, Y), \text{cell}(a, Y))).$$

- Give the respective ordered flattened equations for  $Q$  and  $P$ .
- Give the respective sequences of  $\mathcal{M}_0$  instructions for  $Q$  and  $P$ .
- Execute the compiled code from b). Show also the final state of the HEAP.
- Where is the computed answer substitution (CAS) to be found?

## Exercise 1.2

Consider a more efficient heap representation of  $L_0$  query terms  $q$  where subterms of  $q$  occurring multiple times are represented only once. For example the query  $? - p(a, a)$  shall be represented as

0	STR	1
1	a/0	
2	STR	3
3	p/2	
4	STR	1
5	STR	1

- Give a translation method for  $L_0$  query terms to  $WAM_0$  instructions which produces this heap representation.
- Test your translation with the  $L_0$  query terms

$$? - p(f(a), g(f(a))) \text{ and}$$

$$? - p(f(X, g(a)), f(a, g(X)), f(X, g(a))).$$

### Exercise 1.3

Give the respective sequences of  $\mathcal{M}_0$  instructions for  $\mathcal{L}_0$  query term

$$? - \text{unify}(h(X, f(a)), h(c, f(b)))$$

and  $L_0$  program term

$$\text{unify}(X, X)$$

and execute the compiled code.

### Exercise 1.4

The execution of WAM code may lead to indirections in the heap representation of variable bindings which necessitate the auxiliary function  $\text{deref}(a:\text{address})$ . For example address  $k$  in the following heap structure needs to be dereferenced twice before obtaining an unbound variable cell:

i	REF	j
	⋮	
j	REF	j
	⋮	
k	REF	i

Give an  $L_0$  query term and an  $L_0$  program term such that the execution of the compiled  $\mathcal{M}_0$  code produces a heap structure which needs to dereference at least twice when reading the computed answer substitution (CAS) for one of the variables of the query term.