

Maschinelles Übersetzen natürlicher Sprachen

5. Übungsblatt

2014-11-13

Aufgabe 1

Using the context-free grammar in Figure 1, give a leftmost derivation, and the corresponding parse tree and abstract syntax tree for the sentence “I fly to Alaska”.

S	→	NP VP
NP	→	Pronoun Proper-Noun Det Nominal
Nominal	→	Noun Nominal Noun
VP	→	Verb Verb NP Verb NP PP Verb PP
PP	→	Preposition NP
Noun	→	flight breeze trip morning ...
Verb	→	is prefer like need want fly
Pronoun	→	me I you it ...
Proper-Noun	→	Alaska Baltimore Los Angeles Chicago ...
Det	→	the a an this these that ...
Preposition	→	from to on near ...

Figure 1: Productions of a context-free grammar [JM09, Figs. 9.2. and 9.3, p. 330].

Aufgabe 2

Give a context-free grammar over the terminal alphabet $\{(,), [,]\}$ which represents the well-braced strings over this alphabet (Dyck language). For example, $([])[]$ is well-braced, while $([])$ is not.

Aufgabe 3

Let Σ be an alphabet and $t \in U_{\Sigma}$. Formally define the set of positions of t , denoted by $\text{pos}(t)$. A position is a sequence of integers greater or equal than one. Such a sequence describes a (partial) path through the tree starting at the root. The integers determine with which sub-tree to proceed.

Let $p \in \text{pos}(t)$. Formally define the label of t at p , denoted by $t(p)$, and the sub-tree of t at p , denoted by $t|_p$.

Aufgabe 4

Let $q \in [0, 1]$ and let (G, p) be a probabilistic context-free grammar with start symbol S and the following rules and probabilities:

$$\begin{aligned} S &\rightarrow SS \quad \# q \\ S &\rightarrow a \quad \# 1 - q \end{aligned}$$

1. Find (recursive) definitions for the number of derivations for a^n and the probability $P(a^n | (G, p))$ where $n \geq 1$.
2. Show that (G, p) is consistent iff $q \leq 0.5$. (*Hint*: Don't get distracted by the solution of the first task.)

References

- [JM09] Daniel Jurafsky and James H. Martin. *Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition*. Prentice Hall, Upper Saddle River, NJ, USA, second edition edition, 2009.